

RAMAKRISHNA MISSION VIDYAMANDIRA

(Residential Autonomous College under University of Calcutta)

B.A./B.Sc. SECOND SEMESTER EXAMINATION, MAY 2014

FIRST YEAR

COMPUTER SCIENCE(Honours)

Date : 23/05/2014

Time : 11 am – 2 pm

Paper : II

Full Marks : 75

[Use a Separate Answer Book for each group]

Group – A

1. Answer **any one** from the following : [1×5]
- a) Suppose $a[n][m]$ be a two-dimensional array having n number of rows and m number of columns. Establish an address calculation formulae to compute the location of $a[i][j]$ using column-major order. [5]
- b) A letter means Push and an asterisk means pop in the following sequence of operations over a stack. Give the sequence of values returned by the pop operations when this sequence of operations is performed on an initially empty stack.
E A S * Y * Q U E * * * S T * * * I O * N * * *
Show the stack after each push and pop operations. [5]

Answer **any three** from the following :

2. a) Briefly, differentiate between ADT and Data-structure. [3]
b) Develop an ADT for FRACTION. [7]
3. a) Write an algorithm to convert and infix expression to postfix expression. [6]
b) Convert the following expression from infix to pre-fix form. [2]
 $A / B^C + D * E - A * C$
c) What do you mean by symmetric condition in case of double linked list. [2]
4. a) Write an algorithm to perform binary search (in recursive way) over a list of sequential elements, write down best case, average case and worst case time complexity of binary search? [3+2]
b) Explain how insertion and deletion operations can be performed in $O(1)$ time on circular linked list. [5]
5. a) Critically comment : “Number of inversions measure the unsortedness”. [2]
b) Give an array which has just been partitioned by the first step of quick sort :
3, 0, 2, 4, 5, 8, 7, 6, 9
which of these elements could be the Pivot? Give reasons for your claim. [8]
6. a) $ABC + *CBA - +*$ is a post fix expression with the assumption $A = 1$, $B = 2$ and $C = 3$. Compute the final value obtained if the expression is evaluated. [2]
b) Give the linked representation for the following sparse matrix : [5]
- $$\begin{pmatrix} 0 & 0 & 11 & 0 & 13 \\ 12 & 0 & 0 & 0 & 0 \\ 0 & -4 & 0 & 0 & -8 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$
- c) With an example, show how does interpolation search find an element using minimum number of comparisons. [3]

Group – B

Answer **any four** from the following :

7. a) If $f(x) = 4\cos x - 6x$, find the relative percentage error in $f(x)$, for $x = 0$, if the error in $x = 0.005$. [3]
b) Prove that the sum of Lagrangian functions or co-efficients is unity. [3]
c) Find the value of $f(x)$ at $x = 0$, using appropriate interpolation formula from given following table [4]
- | | | | | |
|----------|----|----|----|----|
| x : | -1 | -2 | 2 | 4 |
| $f(x)$: | -1 | -9 | 11 | 69 |

8. a) Prove that $\Delta \cdot \nabla = \Delta - \nabla$ where, Δ and ∇ holds their usual meaning. [2]
 b) Explain the geometrical meaning of Simpson's one-third rule. [3]
 c) Evaluate $\int_3^7 x^2 \log x \, dx$ by using trapezoidal rule taking $n = 4$, correct upto five decimal places. [5]
9. a) Write down the algorithm of Secant Method. [3]
 b) What is the procedural difference between Regula-Falsi and Secant Method? [2]
 c) Find a real root of the equation $f(x) = x^3 - 2x - 5 = 0$ using regular falsi method. Correct upto three decimal places. [5]
10. a) Compute the values of the unknown in the following system of equations by Gauss-Seidel iterative method. [5]
 $4x - y + z = 7$
 $4x - 8y + z = -21$
 $-2x + y + 5z = 15$
- b) Compute $y(0.2)$, from the equation $\frac{dy}{dx} = x - y$, given $y(0) = 1$, taking $h = 0.1$, by fourth order Range-Kutta Method, correct to five decimal place. [5]
11. a) Define the following terms : [2]
 (i) Basis (ii) feasible solution
- b) Check whether the vectors (2, 4, 10) and (3, 6, 15) are linearly dependent or not. [2]
- c) The owner of a small machine shop has four machinists available to assign to jobs for the day. Five jobs are offered with expected profit for each machinist on each job as follows :

	A	B	C	D	E
1	62	78	50	101	82
2	71	84	61	73	59
3	87	92	111	71	81
4	48	64	87	77	80

Find the assignment of machinists to jobs that will result in a maximum profit. (State each step) [6]

12. a) Find the dual of the following linear programming problem : [3]
 Maximize $z = 2x_1 + 3x_2 + 4x_3$
 Subject to $x_1 - 5x_2 + 3x_3 = 7$,
 $2x_1 - 5x_2 \leq 3$,
 $3x_2 - x_3 \geq 5$,
 $x_1, x_2 \geq 0$

and x_3 is unrestricted in sign.

- b) A steel company has three open hearth furnaces and five rolling mills. Transportation cost (rupees per quintal) for shipping steel from furnaces to rolling mills are shown in the following table : [7]

	M ₁	M ₂	M ₃	M ₄	M ₅	
F ₁	4	2	3	2	6	8
F ₂	5	4	5	2	1	12
F ₃	6	5	4	7	7	14
	4	4	6	8	8	

Find the initial basic feasible solution using Vogel's Approximation Method.

Find also the optimal shipping schedule.

